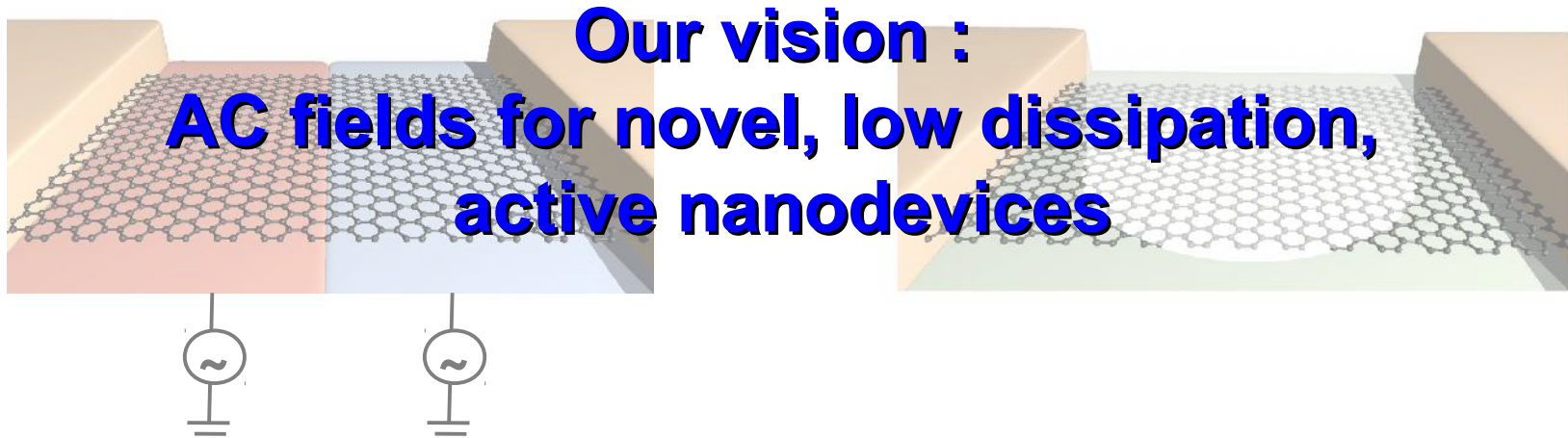


# Tuning the transport properties of graphene through AC fields

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Luis E. F. FOA TORRES

Graphene 2012, Brussels  
April 2012



## Why ac fields?

### control

conductance  
noise

### novel phenomena

quantum pumping  
laser-induced gaps  
Floquet topological insulators

### applications

LFT, PRB 72, 245339 (2005).

LFT and Cuniberti, APL 94, 222103 (2009).

Rocha, LFT and Cuniberti, PRB 81, 115435 (2010);

Rocha, Pacheco et al. EPL (2011)

LFT, Calvo, Rocha, and Cuniberti, APL 99, 092102 (2011).

Ingaramo and LFT, to be published.

Luis Foa Torres

...

Calvo, Pastawski, Roche and LFT, APL 98, 232103 (2011).

Calvo, Pastawski, Roche and LFT, to appear (2012).

Suárez-Morell and LFT, to be published.

S. V. Syzranov, M. V. Fistul, and K. B. Efetov, PRB 78, 045407 (2008).

T. Oka and H. Aoki, PRB 79, 081406(R) (2009) “*Photovoltaic Hall effect in graphene*”

*microwaves*

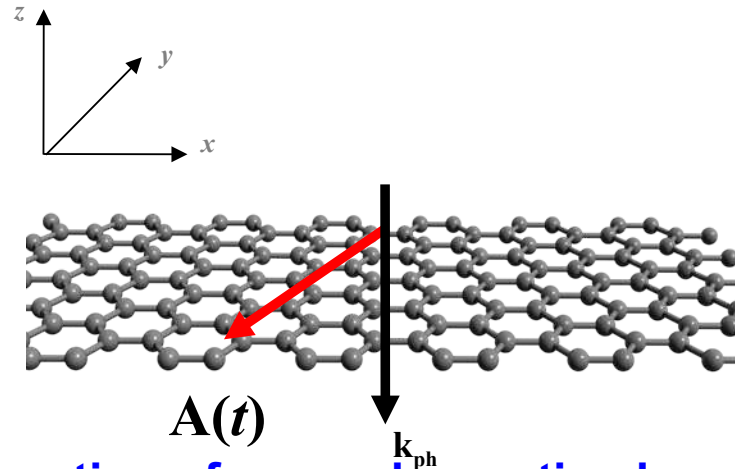
*visible light*

## **Could a laser induce a measurable gap in graphene?**

**How and for which frequencies / intensities / polarization?**

**Idea: Exploit the low dimensionality and the peculiar electronic structure of graphene.**

# Overview of the simulation scheme



Hernán Calvo

**Semi-classical propagation of monochromatic plane waves:**

$$\mathbf{A} = \text{Re } \mathbf{A}_0 \exp[i(\mathbf{k} \cdot \mathbf{r} - \Omega t)]$$

$$A_0 = \frac{E}{\Omega} (1, e^{i\varphi})$$

**Intensity and polarization**

**Hamiltonian model for the electronic structure: k.p, tight-binding**

$$\hat{\mathbf{k}}' \rightarrow \hat{\mathbf{k}} - \frac{e}{\hbar} \mathbf{A}$$

**Floquet theory for the solutions**

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# Brief Summary of Floquet Theory

$$\left[ \hat{H}(x, t) - i\hbar \frac{\partial}{\partial t} \right] \phi_\alpha(x, t) = \varepsilon_\alpha \phi_\alpha(x, t)$$

$$\hat{H}_F(x, t)$$

Floquet Hamiltonian

Floquet (Sambe) space

Usual Hilbert space

$$\rightarrow \mathbf{R} \otimes \mathbf{T} \leftarrow$$

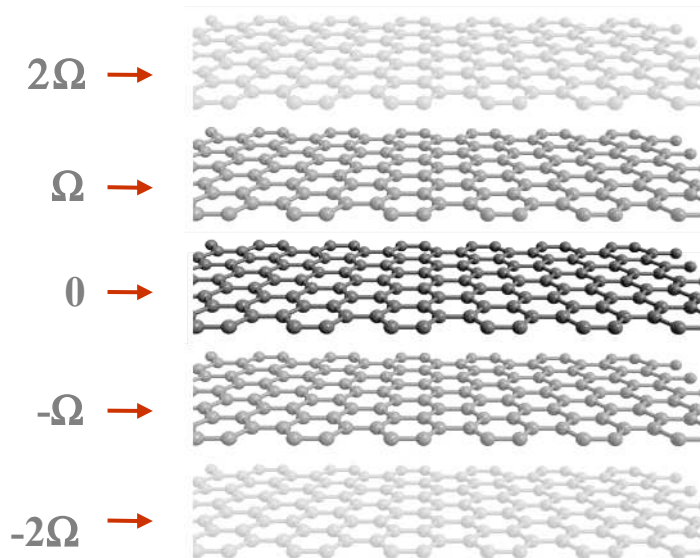
Space of T-periodic functions

Then use Floquet theory approach for driven transport:

S. Camalet *et al.*, PRB 70, 155326 (2004);

S. Kohler, J. Lehmann and P. Hänggi, Phys. Rep. 406, 379 (2005).

L. Foa Torres, PRB 72 245339 (2005)



# Laser-induced gaps in the Floquet spectra

$$N(\varepsilon) = -\frac{1}{\pi} \text{Im} \left\{ \text{Tr} (\mathbf{G}_F(\varepsilon))_{0,0} \right\}$$

For visible light: effects are too small,  
the required gate voltages as too large...

Mid-infrared laser,  $\lambda = 8 \mu\text{m}$

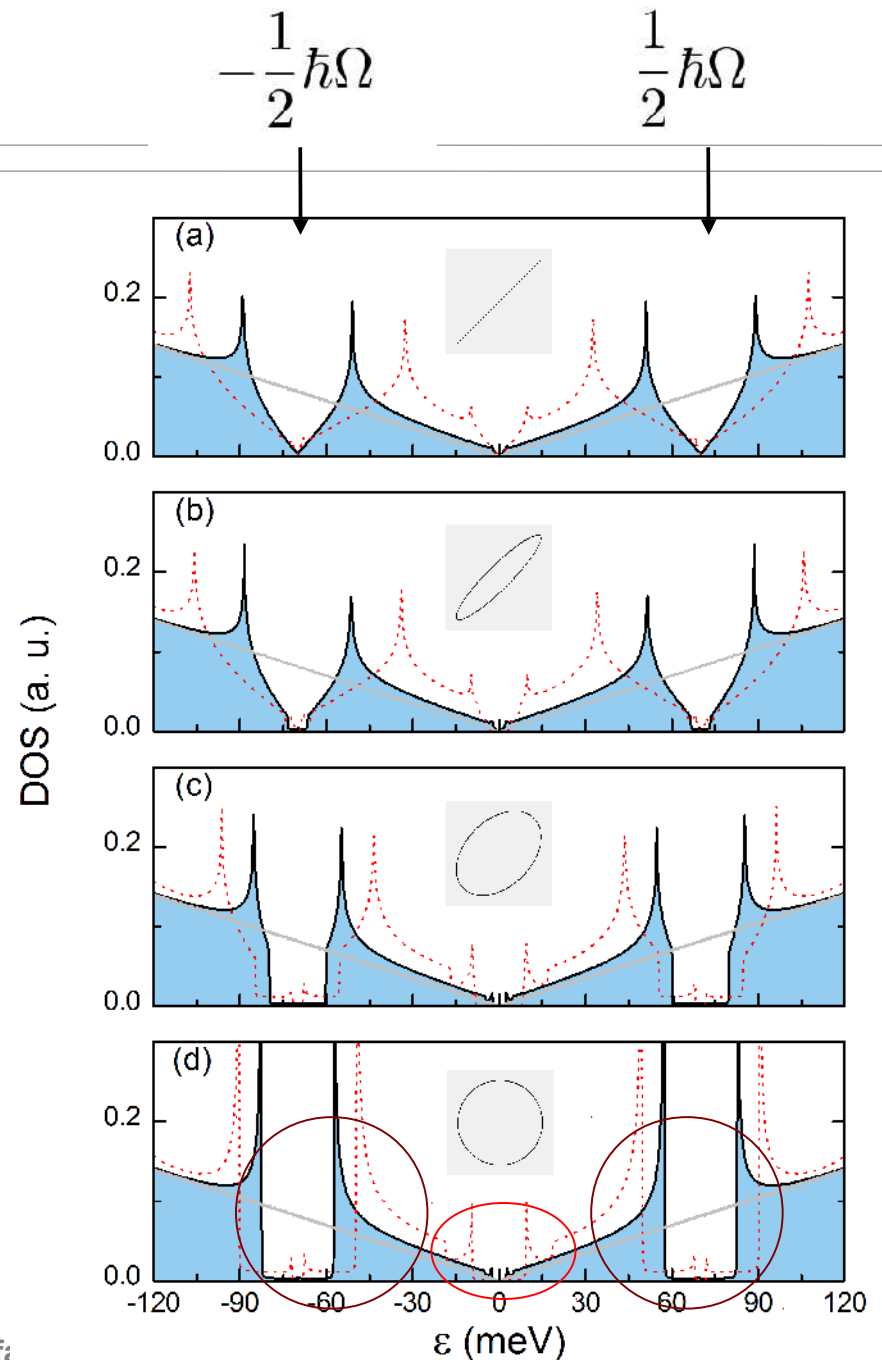


# Laser-induced gaps

$$N(\varepsilon) = -\frac{1}{\pi} \text{Im} \left\{ \text{Tr} (\mathbf{G}_F(\varepsilon))_{0,0} \right\}$$

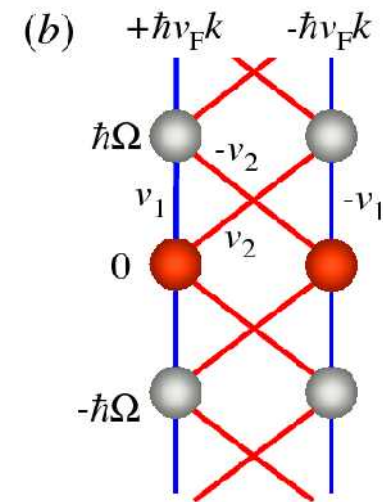
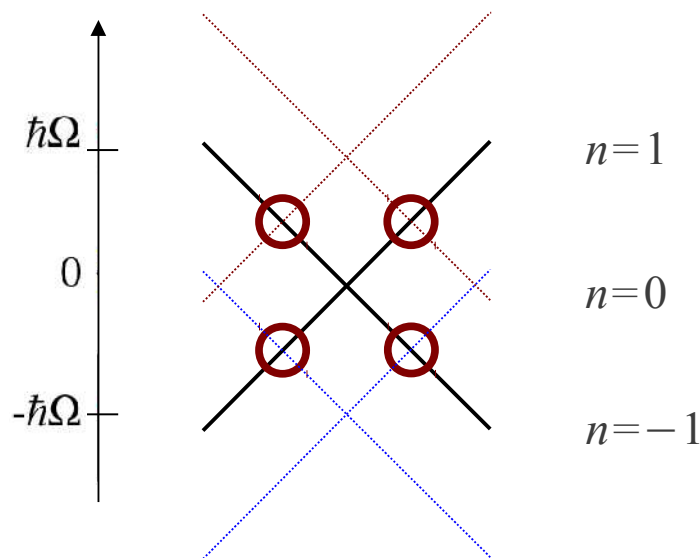
Gaps evolve with polarization

They appear at  $\pm \hbar\Omega/2$   
and at the Dirac point (pseudogap)





# Simple picture for laser-induced gaps



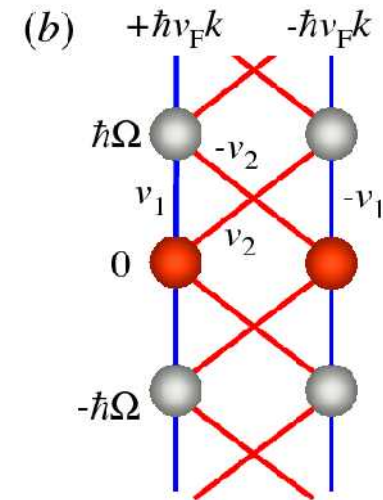
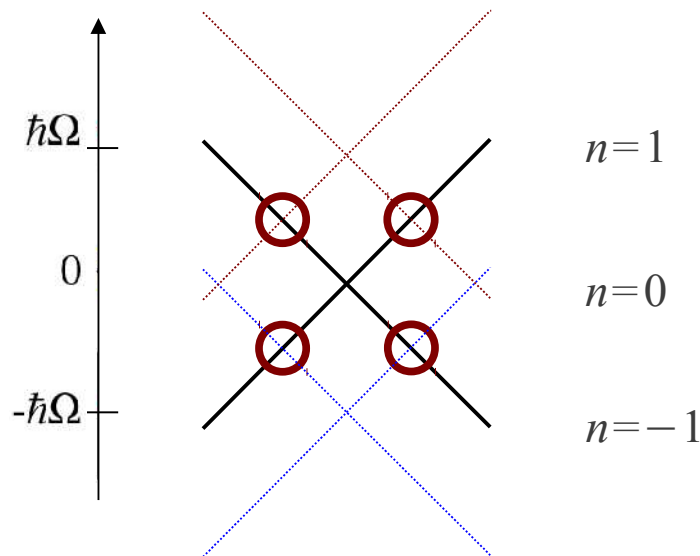
**Inelastic Bragg reflection /  
Lifting of degeneracies in Floquet space**

$$v_1 = \frac{eA_0 v_F}{2} (\cos \alpha + e^{-i\varphi} \sin \alpha)$$

$$v_2 = i \frac{eA_0 \tilde{v}_F}{2} (e^{-i\varphi} \cos \alpha - \sin \alpha)$$

$$\alpha = \tan^{-1}(k_y/k_x)$$

# Simple picture for laser-induced gaps



**Inelastic Bragg reflection /  
Lifting of degeneracies in Floquet space**

Similar to mechanism in :  
LFT and S. Roche, PRL 97, 076804 (2006);  
LFT, R. Avriller, S. Roche, PRB 2008

$$v_1 = \frac{eA_0 v_F}{2} (\cos \alpha + e^{-i\varphi} \sin \alpha)$$

$$v_2 = i \frac{eA_0 \tilde{v}_F}{2} (e^{-i\varphi} \cos \alpha - \sin \alpha)$$

$$\alpha = \tan^{-1}(k_y/k_x)$$



# Laser-induced gaps

$$N(\varepsilon) = -\frac{1}{\pi} \text{Im} \left\{ \text{Tr} (\mathbf{G}_F(\varepsilon))_{0,0} \right\}$$

## Dynamical Gap

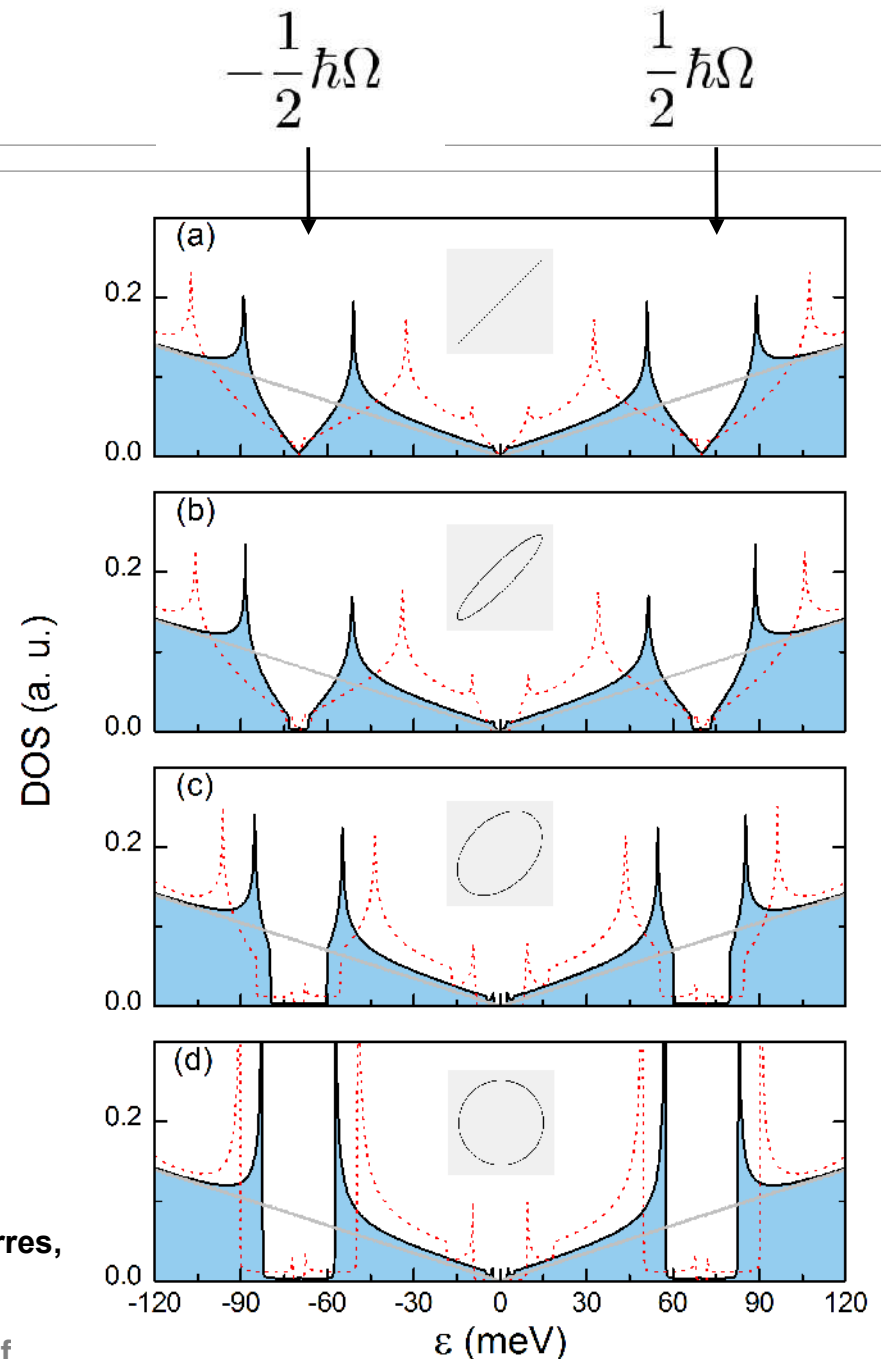
$$\Delta_{k=\Omega/2v_F} \simeq eA_0v_F \sqrt{1 - \cos(\varphi) \sin(2\alpha)}$$

## Dirac Gap

$$\Delta_{k=0} \simeq \frac{8}{\hbar\Omega} \text{Re} \{ \gamma_1 \gamma_2^* \} = 2 \frac{(eA_0v_F)^2}{\hbar\Omega} \sin \varphi$$

Circ. Pol. Oka and Aoki PRB 2009

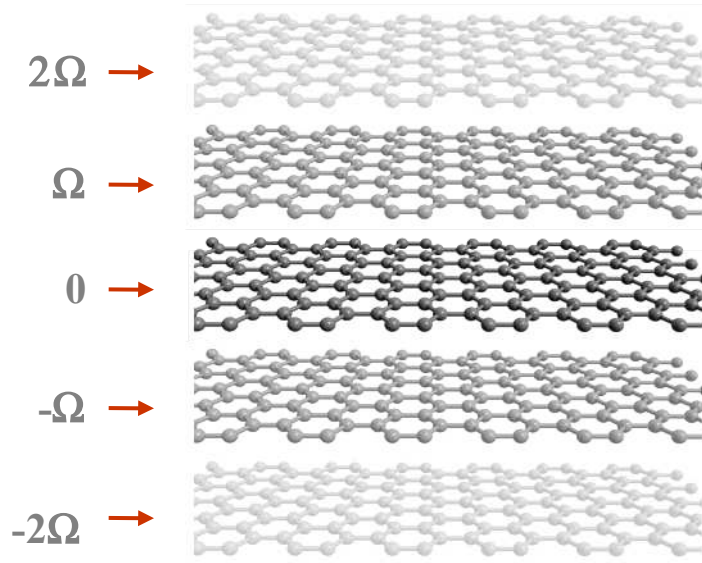
H. L. Calvo, H. M. Pastawski, S. Roche and L. E. F. Foa Torres,  
Appl. Phys. Lett. 98, 232103 (2011)



**What about the influence on transport?**

**Observable effects of these gaps in the  
Floquet spectra ?**

## Tight-binding model and Floquet space ( $\mathbf{R} \times \mathbf{T}$ )



The ac field is included through the Peierls substitution

$$v_{ij}(t) = \gamma_0 \exp \left[ i \frac{2\pi}{\phi_0} \int_{r_i}^{r_j} \mathbf{A}(t) \cdot d\mathbf{r} \right]$$

We use the **Anger-Jacobi expansion**

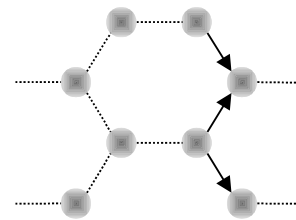
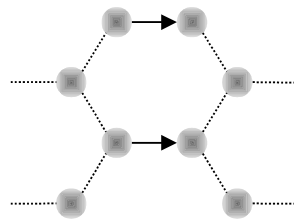
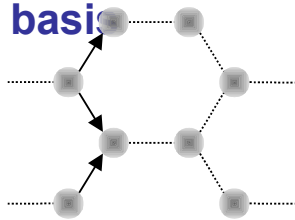
- $m$  – Absorbed or emitted photons

$$t_{\pm \pm}^m = \gamma_0 \sum_k i^k J_k(\pm z_x) J_{m-k}(\pm z_y)$$

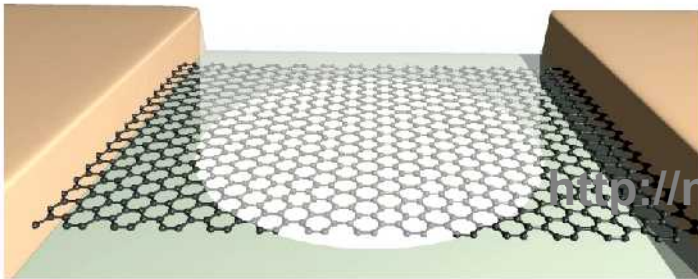
$$z_x = \frac{\pi a A_x}{\phi_0}$$

$$z_y = \frac{\sqrt{3} \pi a A_y}{\phi_0}$$

We choose  $A_x = A_0$  y  $A_y = 0$ , in order to decompose  $H_F$  in the transversal momentum basis

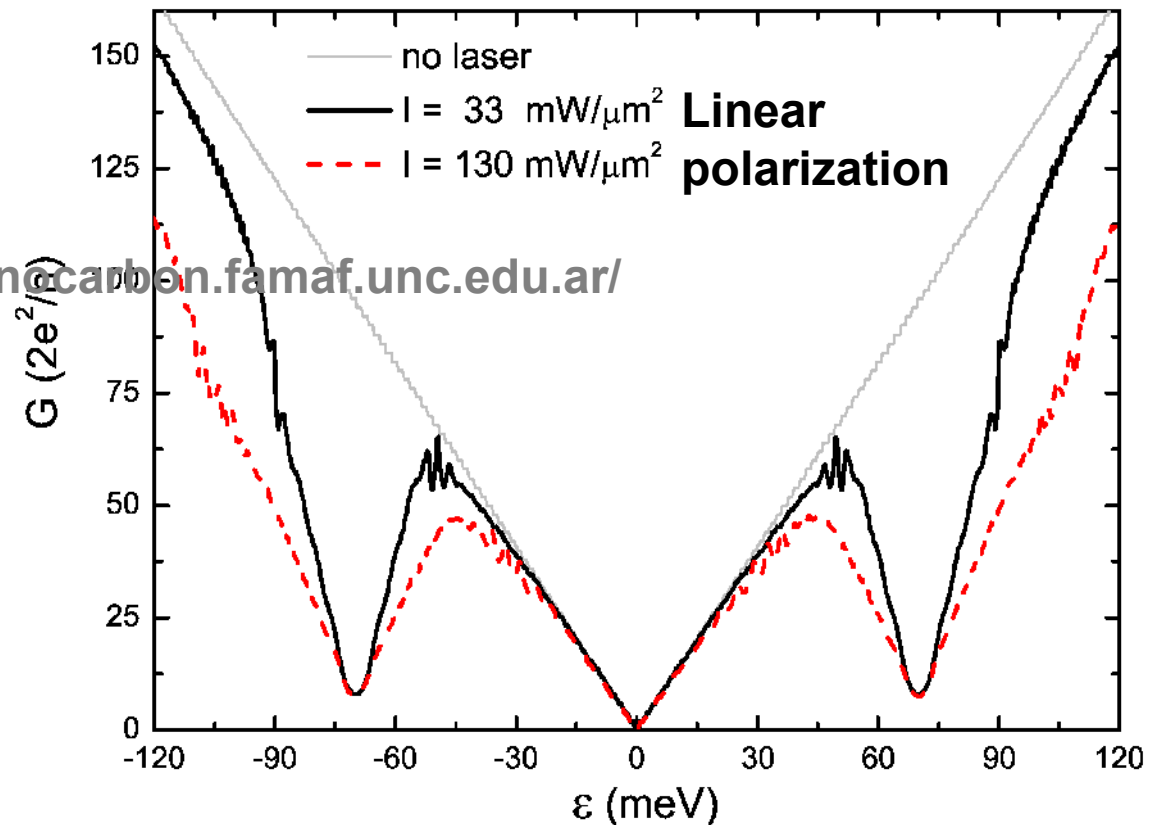


# Radiation effects on the dc Conductance



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- armchair
  - $1\mu\text{m} \times 1\mu\text{m}$  size (!)
  - no dissipation in the sample
  - no radiation in the leads
- Mid-infrared laser ( $\lambda=8\mu\text{m}$ )



Depletion areas mimic what we showed for the DOS.

# What about nanoribbons?

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# Power and Temperature dependence

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# A laser-induced Topological Insulator?

*“Floquet topological insulator in semiconductor quantum wells”*

Netanel H. Lindner, Gil Refael and Victor Galitski  
Nature Physics 7, 490 (June 2011).

*“Transport properties of nonequilibrium systems under the application of light: Photoinduced quantum Hall insulators without Landau levels”*

T. Kitagawa, T. Oka, A. Brataas, L. Fu, E. Demler,  
PRB 84 235108 (Dec. 2011).

Can be verified as well by:

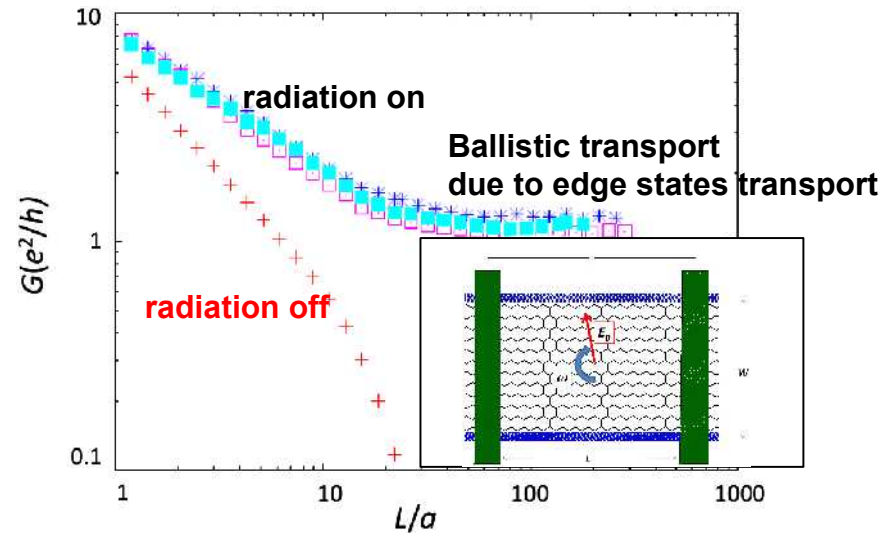
- Calculation of effective Hamiltonian.

+

- Calculation of the associated Chern number, which gives 1 for circular polarization.

Eric Suárez Morell and LFT, to be published.

Evanescent transmission in irradiated system.



Zhengkao Gu, H.A. Fertig, Daniel P. Arovas, Assa Auerbach  
PRL 107, 216601 (Nov. 2011)

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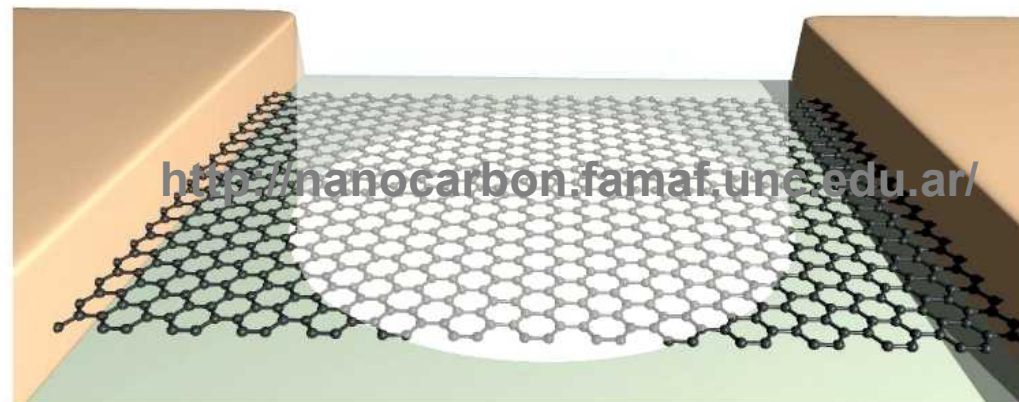
## Conclusions

**Our simulations show that laser fields in the *mid-infrared* can be used to induce tunable gaps in the electrical response of graphene. First atomistic simulations of the transport response.**

**Key ingredients: low dimensionality, peculiar electronic structure,  
» non adiabaticity**

**Possibility of inducing a topological insulator.**

Related publications available at :  
<http://nanocarbon.famaf.unc.edu.ar/>





Universidad Nacional de Córdoba



Thank you!  
Gracias!



Hernán Calvo



Horacio Pastawski



Stephan Roche



G. Cuniberti



Claudia Rocha



Lucas Ingaramo



Pablo Pérez Piskunow



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